



# A wide-angle shift-free metamaterial filter design for anti-laser striking application



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## ABSTRACT

Laser striking is a growing safety concern for pilots and aircraft passengers and there is a great need to develop a wide-angle and shift-free laser filter and protection device. This paper presents one of such design that can effectively block out a Class 3B 532 nm green laser with an Optical Density (OD) of 1.88+ for all polarisation states over a wide range of incident angles up to 85 degree. The design consists of anti-reflection layer, active blocking and substrate layers. The central active blocking layer is designed to be a metamaterial composite media made of silver nanoparticles (AgNP) organised in a three-dimensional (3D) primitive hexagonal Bravais lattice configuration and embedded in a high-index dielectric of Zinc Sulphide (ZnS). The designed filter can be placed onto a number of devices ranging from personnel goggles to aircraft windows. The work may lead to the realisation of next generation laser protection devices that are currently sought by major aerospace companies and government defence agencies.

## 1. Introduction

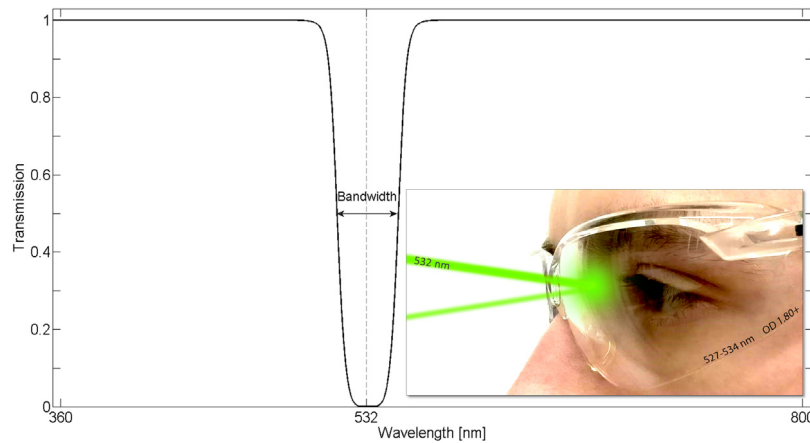
Over the past decade, visible lasers have become a serious risk to aircraft and other transportation vehicles due to the ease of accessibility and low cost of ownership. Recent reports from the Federal Aviation Administration (FAA) and their British counter part, Civil Aviation Authority (CAA), have illustrated that visible laser attacks from green (532 nm) lasers make up 83%–91% of all reported incidents [1,2], with some of the most powerful laser attacks involving diode-pumped solid-state (DPSS) lasers [3]. The resulting damage caused from these attacks are mainly associated with laser eye dazzle [4,5], which describes the temporary impairment to the human eye caused from lasing light within the visible wavelengths. However, exposure for even a short time at the visible radiation range can produce retinal and photo-chemical damage to the eye, and even cause thermal damage to skin [6]. An increased risk of these laser occurrences is that the lasing light could be incident from any angle. Traditional thin-film optics (Rugate notch filters) are currently used to protect against lasers [7–9], and comprise of interference band filters organised as multiple thin coating layers of high and low refractive index dielectric films on a desired substrate [10]. This technology can provide high optical density (typically 4OD+ to 8OD+) and allows for the blocking wavelength to be tailored according to the requirements [11]. However, Rugate filters have disadvantages

especially with angular intolerance. As the angle of incidence increases, the transmission spectrum of the filter experiences a continuous blue-shifting to shorter wavelength [12], causing the failure of the device to operate at desired blocking wavelength. To circumvent this issue, the existing solution in Rugate filter design is to increase the bandwidth of the stop band. This in turn leads to problems including reduced visibility, high colouration and low integrated visual photopic transmission [13]. Companies like Qioptiq, BAE Systems, Boeing, Airbus and government defence agencies have a shared interest in developing a truly wide-angle (up to 60 degree) with shift-free laser blocking and protection device which drives this research. Our aim is to employ metamaterial (MM) design concept to solve the challenge and develop the product.

Metamaterials (MMs) are man-made materials that are not found in nature, and are able to gain electromagnetic (EM) characteristics due to the structural arrangement of meta-atoms, or unit cells, organised in a repeating pattern, where the meta-atoms are much smaller than the wavelength of interest [14,15]. Band rejection filters designed from MMs are competently able to block EM radiation at certain frequency bands. The earliest works in this area were conducted within the low-frequency bands and consisted of the well-known split ring resonator (SRR) [16,17], following with the emergence of various modifications to this design [18–21]. A simplified design that is now commonly used for band rejection in MM is the ‘fishnet’ design [15], and was first studied, in

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**Fig. 1.** The conceptual aim. The figure indicates the ideal transmission response with the insert showing an artist impression of the optical metamaterial notch filter on personnel goggles, deflecting a 532 nm laser beam (527 nm–534 nm), with a bandwidth smaller than 50 nm.

2008 by Valentine et al., to effectively simplify and streamline the shape of the meta-atom and therefore, reduce the difficulties associated with fabrication [22]. The development of these structures has been greatly researched in the Gigahertz (GHz) and Terahertz (THz) bands [23–26], and has moved towards optical frequency. Manufacturing of large-area optical metamaterials, however, has been and continued as a challenge task. Consequently, measures are taken to simplify the structure, with such arrangements existing as circular disc meta-atoms and spherical particles, where these designs can provide similar performance to the fishnet design [27–29]. Bandstop filters in the near-optical region have been achieved using structured coupled cut-wire designs [30], however, this design does not put forward any claim to wide-angle operation, nor polarisation insensitivity. A wide-angle study within the infrared band was reported in 2010 by Liu et al. [31]. Though, this article demonstrated a shift-free perfect plasmonic absorption with zero transmission across the broadband spectrum. The movement to the optical band provides difficulty for wide-angle performance because the MM device requires a sustained resonance at high-frequencies for all angles of incidences. The movement towards 3D metamaterials may provide the solution which has expanded in recent year. One of the earliest examples was demonstrated using a multilayers metal–dielectric fishnet metamaterial [32]. Such devices enabled for a stronger magnetic activity and varying backward phase propagation. Additionally, a much lower transmission rate was achieved with 3D metamaterial filter [32,33]. The research outlined in this paper puts forward a 3D metamaterial design for polarisation-insensitive wide-angle metamaterial band rejection filter to block out a class 3B 532 nm wavelength green light laser based on plasmonic nanoparticles. In the following, the filter parameters were firstly introduced. The metamaterial design was then presented and theoretical formulations for design parameter determinations were given, followed by the simulated device performances, discussions on manufacturing issues and final conclusions.

## 2. Filter design parameters

The desired anti-laser filter will be measured by angular performance of key parameters including transmission spectrum  $T(\lambda)$ , Optical Density (OD), Integrated Visual Photopic Transmission (IVPT) and Colouration, under different polarisation states. These goal parameters are defined as follows.

### 2.1. Transmission spectrum $T(\lambda)$ and optical density (OD)

An ideal transmission response of the blocking device is illustrated in Fig. 1, with an insert demonstrating an artistic impression of an anti-laser filter and its optical filtering capability to block out a 532 nm

wavelength green laser whilst passing through all other wavelengths, whilst attaining an overall high transparency. The Blocking performance of the filter can be measured from the optical density (OD), and is defined as:

$$OD = -\log_{10}(T(\lambda)) \quad (1)$$

The optical density is defined as the degree to which a medium impedes transmitted light waves, and is commonly used within the optical industry to define laser safety guidelines. Our design filter will block out a central wavelength of 532 nm (527 nm–534 nm), with a bandwidth smaller than 50 nm.

### 2.2. Integrated visual photopic transmission (IVPT)

The IVPT is the function associated with the average spectral sensitivity of the filter in accordance to the typical human visual perception, given by (Eq. (2)). The importance of this is to understand how the human eye will interact visually with the filter.

$$IVPT = \frac{\int_0^\infty I(\lambda)V(\lambda)T(\lambda)d\lambda}{\int_0^\infty I(\lambda)V(\lambda)d\lambda} \quad (2)$$

where  $I(\lambda)$  is the spectrum illumination CIE-D65 (daylight),  $V(\lambda)$  is the photopic response of the human eye and  $T(\lambda)$  is the transmission spectrum of the filter ( $0 \leq T \leq 1$ ).

### 2.3. Optical colouration

All optical notch filters will experience a degree of functional visual impairment. The visual impact of an optical filter is a relation to the loss of transmission (IVPT) and the colouration. For analysis of the anti-laser filter, the standard colour map (CIE 1931 *Standard Observer*) will be used. Due to individual variation of the human eye, the distribution of cones in the eye result in the tristimulus values being dependent on the observer's field of view. The CIE 1931 colour map represents a chromatic response for the average human within a 2° arc inside the fovea centralis, a region of closely packed cones in the eye; thus, providing the user confidence of the colouration response. The transmission and reflective cases can be established from Eqs. (3) and (4).

$$X = \int_0^\infty I(\lambda)T(\lambda)\bar{x}(\lambda)d\lambda \quad (3a)$$

$$Y = \int_0^\infty I(\lambda)T(\lambda)\bar{y}(\lambda)d\lambda \quad (3b)$$

$$Z = \int_0^\infty I(\lambda)T(\lambda)\bar{z}(\lambda)d\lambda \quad (3c)$$

where  $I(\lambda)$  and  $T(\lambda)$  is same as those in above (Eq. (2)), and  $\bar{x}(\lambda)$ ,  $\bar{y}(\lambda)$  and  $\bar{z}(\lambda)$  are colour matching functions that numerically describe the chromatic response of the observer.

The translation to the  $x$ - $y$  coordinates on the colour map are described by Eq. (4).

$$x = \frac{X}{X + Y + Z} \quad (4a)$$

$$y = \frac{Y}{X + Y + Z} \quad (4b)$$

### 3. Results and discussions

#### Proposed design

We have use plasmonics and AR coating theory to develop the filter design. Fig. 2 shows the proposed anti-laser notch filter design that shows wide-angle and polarisation insensitive properties at 532 nm wavelength. The design consists of three layers: anti-reflection (AR, top), active blocking (AB, middle) and substrate layers (bottom). The active layer in the middle is a 3D artificial media made of silver nanoparticles (AgNP) organised in a primitive hexagonal Bravais lattice planar array form and embedded in a surrounding dielectrics. We select AgNP as main active element because of its flexibility in its resonance engineering: its peak position, bandwidth and transmission rate can be well tuned by size, surrounding medium and 3D configuration. The hexagonal 3D arrangement was chosen as it boosts device's angular performance. The AgNP size was fixed at 9 nm (diameter) in the design. This follows the design requirement of narrow blocking bandwidth of less than 50 nm (Fig. 1). However, at 9 nm diameter the AgNP dielectric constant deviates from it bulk and needs to be corrected. This was achieved by including a size correction factor in the design process. Finally, the AR layer is deposited on the top of the active blocking layer to ensure beams outside of the blocking band (e.g daylight) are able to pass through the device at a high transmission rate. This is important to ensure that device has a clear visibility while blocking out the 532 nm laser beam.

#### Design theory and process

Our basic design theory is plasmonics, namely plasmon resonance of silver nanoparticles (AgNP). A coupled design approach involving both analytical theory and numerical simulation was used. We use analytical theories (e.g. Mie theory and thin-film interference theory) as base to find approximate design parameters and subsequently use full-wave numerical simulation software CST Microwave Studio to tune and verify them to meet the design targets. The optical properties for refractive indices and extinction coefficients have been obtained from literature [34–36] and patched for small AgNPs as discussed above and in [37]. The light propagation direction,  $k$  vector, with normal incident is perpendicular to the design facets. The electric field,  $E$ , is directional to the  $y$ -axis and the magnetic field,  $H$ , is directional to the  $x$ -axis, and initiated for the required transverse modes. The wave propagation angle,  $\theta$ , has been adjusted accordingly to compute the  $k$  vector at various angle of incidence. A generalised design approach is finally developed, which can be used to find filter parameters for any blocking wavelength within the visible band. We use 532 nm as a particular example in this paper, but other wavelengths such as 450 nm and 613 nm are easily achievable as well.

**Determination of host medium for AgNP:** The active layer consisting of a 3D primitive hexagonal Bravais lattice of 9-nm-diameter AgNP. The composite's effective refractive index (Fig. 3) can be determined from the Maxwell-Garnett formula (Eq. (5)), which defines the bulk effective permittivity of the metal-dielectric composite [38], and relationship between refractive index and permittivity (Eq. (6))

$$\frac{\epsilon_{eff} - \epsilon_h}{\epsilon_{eff} + 2\epsilon_h} = f \frac{\epsilon_m - \epsilon_h}{\epsilon_m + 2\epsilon_h} \quad (5)$$

$$\bar{n}^2 = (n + ik)^2 \equiv \epsilon_{eff} = \epsilon_r + i\epsilon_i \quad (6)$$

$\epsilon_{eff}$  represents the effective permittivity with its respective complex notation,  $\epsilon_m$  and  $\epsilon_h$  signifies the permittivity for Ag and the dielectric host respectively, and  $n$  and  $k$  denote the refractive index and extinction coefficient. An additional term has been added to the classical Drude dampening frequency,  $\gamma_{particle} = \gamma + (v_F / (\alpha r_p))$  to compensate for the particle becoming smaller than the free mean path of the electron (for silver the bulk mean free path at room temperature is about 53 nm [39]);  $\gamma$  and  $\gamma_{particle}$  represents the dampening frequency of the bulk metal and new dampening frequency according to the particle size ( $r_p$ ), with relation to the Fermi velocity ( $v_F$ ) and  $\alpha$ , where due to the spherical nature of the particles  $\alpha = 4/3$ . Accordingly, the particle size has been taken into consideration for this design (see Fig. 3).

Once the effective refractive index of active layer was determined, we use following equation to find the notch location, according to the plasmonic material and surrounding medium;

$$\lambda_t = e^{\frac{c_1 + Re[n_{host}]}{c_2}} - \sigma \quad (7)$$

where  $\lambda_t$  is the desired wavelength and is equal to the wavelength associated to the peak value of the extinction coefficient ( $k$ ) of the active layer.  $\lambda_t = 532$  nm when  $Re[n_{host}] = 2.382$  and  $\sigma =$ . The  $c$  values are the coefficients of Silver ( $c_1 = 18.741$  and  $c_2 = 3.3654$ ),  $n_{host}$  is the refractive index of the surrounding dielectric medium and  $\sigma$  is a particle size correction function ( $\sigma = 1.24$ ). This formula applies to all other wavelengths. For example, if the desired wavelength was to block out a 450 nm blue laser, the surrounding dielectric medium would need a refractive index of  $n = 1.82$  instead.

**Determine particle spacing:** The blocking bandwidth ( $\Delta\lambda$ ) is affected by both the AgNP particle size and its 3D hexagonal lattice array density. The Q-factor, defined as  $Q = \lambda_t / \Delta\lambda$ , was used to calculate for the blocking wavelength bandwidth. The Q-factor was optimised for high blocking performance while remaining with a minimal bandwidth, resulting in an optimum design of  $\alpha_x = \alpha_y = \alpha_z = \lambda_{laser} / 16$ ;  $\beta_z = 4\alpha_z$  and  $\gamma_z = 3\alpha_z$ , as shown in Fig. 2.

**Determine AR coating and layer thicknesses:** The 532 nm anti-laser device has an active layer that is sandwiched between a glass substrate ( $n = 1.52$ ) and an AR coating layer of Magnesium fluoride ( $MgF_2$ ,  $n = 1.38$ ). The introduction of  $MgF_2$  is to reduce the reflected light intensity and improve the overall transmittance of the device by allowing the natural incident incoherent light to experience a phase difference of  $\pi$ , resulting in destructive interference of the waves. The thin film anti-reflection coating is chosen to match the relationship of the reflection coefficient between air, the active layer and the glass substrate [40], so that:

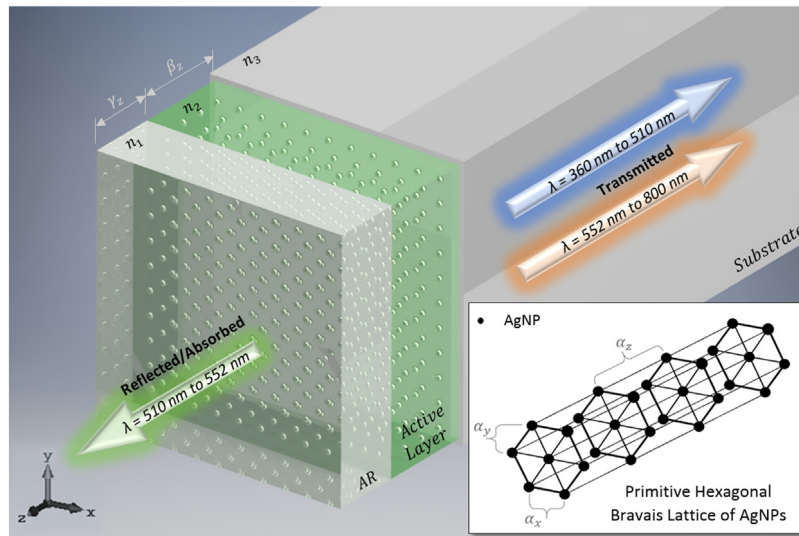
$$n_{AR} \approx \frac{1}{\sqrt{n_{air}/n_{sub}}} \quad (8)$$

The presence of the high-index ZnS positioned next to the low-index substrate, makes it appear that the substrate has a high index, thus, the subsequent layer of  $MgF_2$  becomes more effective as an AR coating [41]. The thickness of the two layer coating design has been formulated from conventional double-layer coating principles and is expressed in Eq. (9).

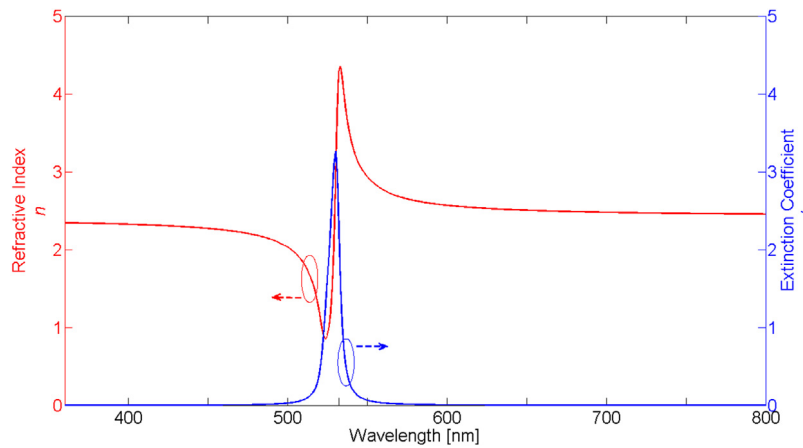
$$\tan^2 \delta_1 = \frac{(n_{sub} - n_{air})(n_{ZnS}^2 - n_{air}n_{sub})n_{MgF_2}^2}{(n_{MgF_2}^2 n_{sub} - n_{air}n_{ZnS}^2)(n_{air}n_{sub} - n_{MgF_2}^2)} \quad (9a)$$

$$\tan^2 \delta_2 = \frac{(n_{sub} - n_{air})(n_{air}n_{sub} - n_{MgF_2}^2)n_{ZnS}^2}{(n_{MgF_2}^2 n_{sub} - n_{air}n_{ZnS}^2)(n_{ZnS}^2 - n_{air}n_{sub})} \quad (9b)$$

where  $\delta$  is a positive real number that satisfies the quarter wavelength relationship and  $n$  is the refractive index of the subscripted materials. Two solutions for each  $\delta$  value will be produced that must be correctly paired, with the  $\delta_1$  component being a relation to the AR coating and the  $\delta_2$  component being a relation to the active layer. However, for this study, the solutions found in Eq. (10a) have been selected to minimise the number of odd multiples of quarter wavelengths and to sufficiently



**Fig. 2.** (a) Configuration of the 532 nm anti-laser device based on three-dimensional hexagonal planar array of AgNP as the active layer with  $\alpha_x = \alpha_y = \alpha_z = \lambda_{laser}/16$ ;  $\beta_z = 4\alpha_z$  and  $\gamma_z = 3\alpha_z$ . Insert shows the hexagonal lattice arrangement of the AgNPs within the ‘active layer’.



**Fig. 3.** The effective refractive index and extinction coefficient for the active layer.

host the required number of AgNP structured lattice layers. Each  $\delta$  solution is multiplied by a reference wavelength,  $\lambda_{Ref} = 275$  nm, to solve for the layer thickness, such that the active layer is approximately equal to  $\lambda_{laser}/4$ .

$$\delta_1/2\pi = 0.1749 \quad \delta_2/2\pi = 0.4803 \tag{10a}$$

and

$$\delta_1/2\pi = 0.3251 \quad \delta_2/2\pi = 0.0197 \tag{10b}$$

In CST simulation, the excitation port of the incident beam was set in the far-field zone of the device, which lies beyond the Rayleigh length  $Z_0$  given by:

$$Z_0 \geq \frac{\pi_0^2}{\lambda} \tag{11}$$

where  $W_0$  is the waist radius of the embedded fundamental Gaussian beam of a frequency-doubled YVO<sub>4</sub> 532 nm laser.

**Simulated filter performance**

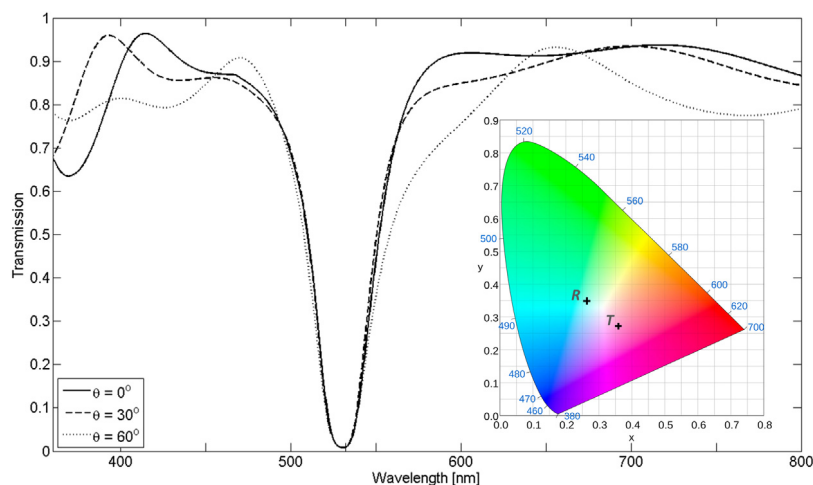
Fig. 4 shows the key result of the designed filter; the transmission response at various incident angles of 0° (solid line), 30° (dashed line) and 60° (dotted line). The dielectric host material, ZnS, tunes AgNP resonance peak from 354 nm (same lattice configuration but with air as host medium) to 530.35 nm. The resulting bandwidth is 41.8 nm at the

full width at half maximum, qualifying the performance of the filter to introduce a band rejection at the 532 nm lasing wavelength, whilst providing high transmission outside of the rejected band. As the incident angle increases, it is clear to see that zero-shift occurs at the rejection band. The blocking at the rejection band continues to 85° of incidence. In reality, the user would only experience the lasing wavelength at varying incident angles. The natural light transmission outside of the 532 nm wavelength would remain at maximum at the angle of the users mid-to-near peripheral vision ( $\theta = 30^\circ\text{--}60^\circ$ ), noted in Fig. 5, whilst the ocular focus would remain at the macular region of the peripheral vision ( $\theta = 0^\circ\text{--}18^\circ$ ). From the wavelengths, outside of the notch bandwidth, of 360 nm to 510 nm and 552 nm to 800 nm, the average transmission across the filter is 81.09% and 89.06%, respectively; with an overall spectral response of 77.87% from 360 nm to 800 nm.

The IVPT response of the discussed filter is 61%. The transmission colouration response exists on the coordinates ( $x = 0.36$  and  $y = 0.27$ ) and the reflection colouration response exists on the coordinates ( $x = 0.26$  and  $y = 0.35$ ) of the standard CIE 1931 colour map. As seen in Fig. 4 insert, the calculated transmission and reflection colouration are close to neutral but experience a slight magenta and turquoise hue, respectively.

Fig. 5 shows the calculated optical density (OD) of the filter for angles between 0 and 85 degree. The OD remains above 1.88 across the whole range of angles. This indicates that the described filter is able to perfectly block a common low power (<76 mW) Class 3B 532 nm DPSS





**Fig. 4.** Transmission of the three-dimensional optical metamaterial filter versus wavelength for incident angle at  $\theta = 0^\circ$ ,  $\theta = 30^\circ$  and  $\theta = 60^\circ$ . The solid, dashed and dotted lines denote the cases of the incident angle. Insert shows the CIE 1931 colour map for the transmission (T) and reflection (R).

laser of continuous-wave operation at all angle of incidence without blue shift occurring. Blocking of <100 mW is achievable between the angles of  $0^\circ$  and  $20^\circ$ . However, despite having zero shift of the notch at the point of resonance, the out of resonance wavelengths begin to attenuate and results in broader bandwidths. This attenuation is greatly augmented beyond the incident angle of  $70^\circ$  and lies within the far peripheral of the human eye. Due to this attenuation, the device design can be labelled as having a critical angle of  $70^\circ$ .

Another factor to consider is the polarisation sensitivity of the optical filter, Fig. 5 illustrates that the results are independent of the incident angle in two polarisation modes p and s. The slight fluctuation between p and s polarisation results for angles between  $45^\circ$  to  $70^\circ$  is a consequence of the Brewster angle of the AR coating,  $\sim 54^\circ$  [42], and is not caused by the active blocking layer of three dimensional AgNP planar array. The variation beyond theta  $70^\circ$  is due to a minor change ( $\sim \pm 1$  nm) in resonance between s and p polarisation.

### Mechanism

The wide-angle shift-free features of the design are resulting from its 3D topological arrangement (primitive hexagonal Bravais lattice) [43] and the excitation of similar resonance modes under different incident angle beams at 532 nm. Fig. 6 shows the power flows of Poynting vector calculated for the 9-nm-diameter AgNP when it is irradiated by 532 nm laser at 0 and 45 degrees for both TE (a, b) and TM (c, d) polarisation incident beams. Under TE wave, the AR layer has a matched phase with Air layer so that angles were preserved at this Air–AR interface. However, the power flows are undergoing a 45-degree rotation to 0-degree when it reaches the AR–AB interface, as shown in (b). As a result, regardless of the angle differences, the power flows passing through the AB layer in (a) and (b) are almost the same, leading to the near-identical field absorption and flow patterns under 0 and 45-degree incidences in the AB layer. This picture holds true for other angles up to about 85 degree and Laser energy was most completely absorbed by three layers of AgNPs in AB media for TE polarisation. This is why multiplayer design has been selected, thus a 3D configuration is important for our work. Under TM wave, however, the situation is slightly different. As shown in (d), the beam rotates by around 45-degree clockwise to 0-degree at air–AR interface, but rotates anti-clockwise back to 45-degree at AR–AB interface, which leads to differences in light absorption between normal (c) and angular incident beams (d), but does not affect the resonance wavelength. Three layers of AgNPs are needed for normal incident beam (c), and 4 layers for 45-degree incident beams (d), to reach desired energy decay level. This suggests TM angular beam is the case we need to look at when decides how many AgNPs layers we need in our design. Nevertheless, regardless of polarisation states, the incident laser energy can be blocked by using 4 layer AgNPs design.

### 4. Discussion

Manufacturing sub 10 nm structures on a complex three-dimensional plane presents several major challenges [44], especially when dealing with large area fabrication. Overcoming the diffraction limit that is experienced with conventional photolithography methods is now made possible with the introduction of block co-polymers (BCP), which have gained significant attraction as a nanoscale self-assembling material [45]. The unique ability of BCPs stems from the tendency to assemble discrete ordered morphologies at equilibrium over a large area [46]. Utilising the ability of the BCP to achieve spot feature dimensions of sub 10 nm [47–49] with a continuously uniform natural period separation could be a progressive move in the fabrication of the described laser protection design. The fabrication process can be enabled with material systems that include PS-b-PMMA, which can exhibit a high-order natural spacing length of 10 nm to 200 nm depending on the annealing process [50]. Two-dimensional periodic and symmetric metasurfaces has previously been demonstrated and reported by Ju Young Kim et al. in 2016, where it was successfully demonstrated that a large area assembly of structured plasmonic materials using block copolymer self-assembly method was possible [51]. Moving towards a three-dimensional array can be achieved with multi-layer thin film BCP's [52,53], and would empower the next generation of complex optical metamaterials for various applications. Another possible approach is to use latest dielectric superlens technology with extremely high spatial resolution (15 nm) coupled with femtosecond laser for direct parallel writing of proposed device in transparent media [54,55].

### 5. Conclusion

Our work explores the advancement of the next generation of laser protection devices and offers a design that is able to block a 532 nm laser, with an optical density of 1.88+. An additional function to this design is its ability to support multiple polarising laser blocking. The filter is designed using a metamaterial concept, where the active band rejection component is of repeated structures much smaller than the wavelength of interest. The considerable advantage to this filter design is the ability to rejects the lasing wavelength at all angles of incident whilst remaining shift-free, unlike the traditional optical thin-film laser protection coatings. Higher optical density can be achieved at the expense of a wider broadband to block pulsed and higher power CW lasers. The transmission of the design from a human's visual perception is  $\sim 61\%$ , with an overall filter spectral transmission of 78%. This research offers a promising avenue for future high-performance laser protection systems that could be used in a wide variety of industries.

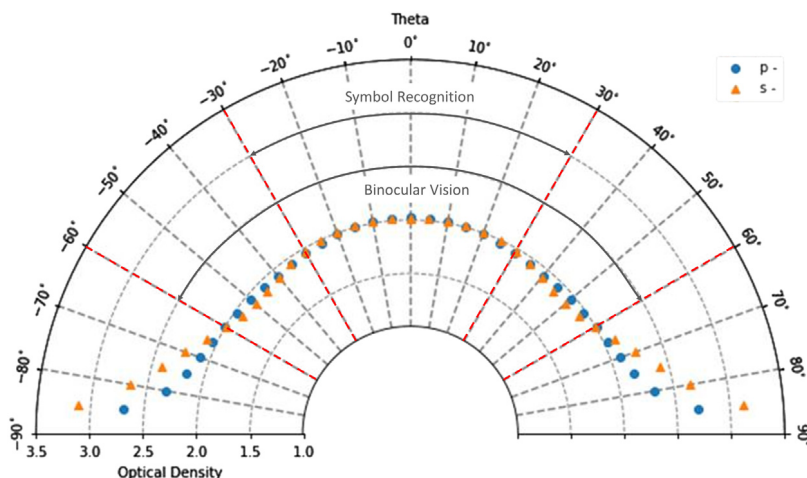


Fig. 5. OD of the designed filter at the laser wavelength of 532 nm. The circle and triangle data points denote the transverse mode of the electromagnetic radiation. Theta represents the angle of incidence. The peripheral vision regions have been noted in accordance to theta.

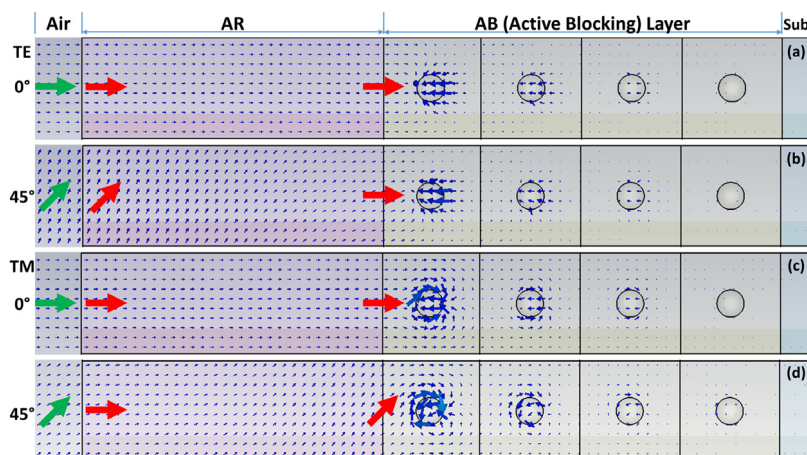


Fig. 6. Power flow plots for (a) TE and (b) TM incident beams at 532 nm wavelength with varying angles of incident of 0 and 45 degrees.

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